

## A.P. Calculus AB Student Manual

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If you do find errors or have any questions or comments, please direct them to: *team@mastermathmentor.com*.

## **Table of Contents (AB Calculus)**

Below are all the topics we will cover in this course. Each topic will have a classwork section where we will work out problems in class and you will take notes. Each section will also have a homework section containing many types of problems you will see on exams and on the A.P. Test.

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(\*) - Not required in AB Calculus